

# Competition



2022/2023 SEASON – FINAL ROUND

You are participating in a TV competition where your goal is to build a sequence whose last element is a given natural number  $n$ . You can reach it sticking to the following rules:

- (1)  $x_0 = 1$ .
- (2)  $x_i = x_j @ x_k$  for each  $i \geq 1$ ,  $0 \leq j, k < i$  and  $@$  is any of the following operations, each of which has a unique code:

Code	Operation
1	$x_i = x_j + x_k$ , addition
2	$x_i = x_j - x_k$ , subtraction
3	$x_i = x_j * x_k$ , multiplication
4	$x_i = x_j / x_k$ , integer division
5	$x_i = x_j \% x_k$ , remainder of division
6	$x_i = x_j \& x_k$ , bitwise "and"
7	$x_i = x_j   x_k$ , bitwise "or"
8	$x_i = x_j \wedge x_k$ , bitwise exclusive "or"

The constraint  $1 \leq x_i < 2^{63}$  must be fulfilled during the whole time.

The application of an operation is denoted by (*operation code*) ( $j$ ) ( $k$ ). The goal is to find a sequence of operations for which  $x_l = n$  and  $l$  is as small as possible.

Answer  $t$  such queries.

## Input

The first line of the file **competition.in** contains the number  $t$ . Each of the next  $t$  lines contains one number -  $n$  for the corresponding query.

## Output

For each query, print in the file **competition.out** first the number of operations  $l$  ( $0 \leq l \leq 150$ ), and on the next  $l$  lines - the operations themselves.  $x_l = n$  must be satisfied. **If for some  $n$  you cannot find the required operations, print -1.**

## Constraints

$$2 \leq n < 2^{63}$$

$$1 \leq t \leq 1000$$

It is guaranteed that for every  $n < 2^{63}$  there is a solution with at most 150 operations.

**Time limit: 5 sec.**

**Memory limit: 256 MB.**

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## Scoring

For each solved query  $l^2$  will be added to your score, and for each  $-1: 300^2$ . For each test, let  $minScore$  be the smallest score among all participants' scores and  $yourScore$  be your score. You will be awarded  $1 - \sqrt{1 - \frac{minScore+}{yourScore+}}$  multiplied by the amount of points for the test.

The tests are distributed as follows:

$\frac{n}{t}$	$< 2^{15}$	$< 2^{31}$	$< 2^{63}$
$= 10^1$	5%	5%	5%
$= 10^2$	5%	15%	15%
$= 10^3$	5%	15%	30%

## Tests generation

The numbers  $n$  are randomly generated in the respective intervals that bound them (each number in the interval has an equal chance). It is guaranteed that they are distinct.

## Sample test

Input (competition.in)	Output (competition.out)
2	10
32	1 0 0
123456789012345678	1 1 0 1 2 0 8 2 3 3 4 4 4 5 1 7 6 5 5 7 6 2 5 8 6 9 5 -1

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## Example explanation

For  $n = 32$ ,  $x_0 = 1$

$$x_1 = x_0 + x_0 = 1 + 1 = 2$$

$$x_2 = x_1 + x_0 = 2 + 1 = 3$$

$$x_3 = x_2 + x_0 = 3 + 1 = 4$$

$$x_4 = x_2^{x_3} = 3^4 = 7$$

$$x_5 = x_4 * x_4 = 7 * 7 = 49$$

$$x_6 = x_5 / x_1 = 49 / 2 = 24$$

$$x_7 = x_6 | x_5 = 24 | 49 = 57$$

$$x_8 = x_7 \% x_6 = 57 \% 24 = 9$$

$$x_9 = x_5 - x_8 = 49 - 9 = 40$$

$$x_{10} = x_9 \& x_5 = 40 \& 49 = 32$$

No solution was found for  $n = 123456789012345678$  and  $-1$  is printed instead.

The total result is  $10^2 + 300^2 = 100 + 90000 = 90100$