

Dominoes

SEASON 2021/2022 – FORTH ROUND



Sashka won't stop playing with her favourite dominoes. She has four types of dominoes (Fig. 1). They have two sides, left and right respectively. Both of the sides are colored in blue or red. For convenience, Sashka denoted them as follows:

- Domino №1: blue-blue
- Domino №2: blue-red
- Domino №3: red-blue
- Domino №4: red-red

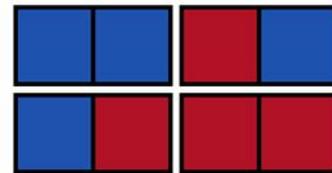


Fig. 1

You should note that blue-red is different from red-blue.

Sashka takes out all the dominoes she has and orders them in a sequence. Sashka denotes a sequence of dominoes as *beautiful* if each adjacent side of the dominoes is with different color. More precisely, if the left side of the i -th domino is l_i and the right is r_i , then for every $1 \leq i \leq N - 1$, $r_i \neq l_{i+1}$. A sample *beautiful* sequence is shown below (Fig. 2).



Fig. 2

In Bulgaria there are T domino sets, where the i -th set contains $d_{i,1}$ dominoes from the first type, $d_{i,2}$ from the second type, $d_{i,3}$ from the third type and $d_{i,4}$ from the fourth type. At first, Sashka took the *intermediate* assessment of a domino set to be the count of different *beautiful* sequences, which can be made from it. Two domino sequences are different if two different dominoes are on the same positions in the sequences. She realized that the count of such sequences could be pretty big, so she changed the method of assessment. The new *intermediate* assessment of a domino set is taken to be the count of achievable *beautiful* sequences modulo $10^9 + 7$. The bigger the remainder is, the better the *intermediate* assessment is for the set, but there is more. Sashka is allowed to recolor K_i dominoes in the i -th set to increase her assessment of the set. Recoloring of a domino in the i -th set goes like this: Sashka chooses two types of dominoes x and y ($x \neq y$, $1 \leq x, y \leq 4$, $d_{i,x} \neq 0$) and decreases $d_{i,x}$ by 1 and increases $d_{i,y}$ by 1 ($d_{i,x} := d_{i,x} - 1$, $d_{i,y} := d_{i,y} + 1$, where $:=$ is the sign for assignment). **So in the end, the final assessment of a domino set is the maximal intermediate assessment of all possible recolorings.** Sashka wants to find the *final* assessment of all dominoes set in Bulgaria, but it'll be hard for her to calculate it by hand. That's why she asks you, as her third cousin, to write a program `dominoes.cpp`, which will find it.

Input

On the first line of `dominoes.in` the number T is given – the number of domino sets in Bulgaria. The i -th of the next T rows contains 5 natural numbers, $d_{i,1}, d_{i,2}, d_{i,3}, d_{i,4}, K_i$ respectively.

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Output

For each of the domino sets, you should print a number in `dominoes.out`, which is its *final* assessment.

Constraints

$$1 \leq T \leq 5$$

$$1 \leq d_{i,1} + d_{i,2} + d_{i,3} + d_{i,4} \leq 120$$

$$0 \leq d_{i,1}, d_{i,2}, d_{i,3}, d_{i,4} \leq 120$$

$$0 \leq K_i \leq 20$$

$$\text{For every } 1 \leq i, j \leq T, d_{i,1} + d_{i,2} + d_{i,3} + d_{i,4} = d_{j,1} + d_{j,2} + d_{j,3} + d_{j,4}$$

Time Limit: 1 sec.

Memory Limit: 256 MB.

Sample testcases

Input (<code>dominoes.in</code>)	Output (<code>dominoes.out</code>)
3 1 1 1 0 0 1 0 1 1 0 3 0 0 0 2	1 3 3
3 3 3 3 1 3 8 1 1 0 4 10 0 0 0 5	120 40 5
2 9 2 5 10 5 9 8 4 5 3	3171168 2944656
3 30 30 30 30 20 30 60 15 15 20 60 60 0 0 20	999079969 997861536 0

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Explanation of the sample testcases

For the first testcase:

- For the first domino set the only possible sequence is:



Fig. 3

- For the second domino set, the three possible sequences are the following:

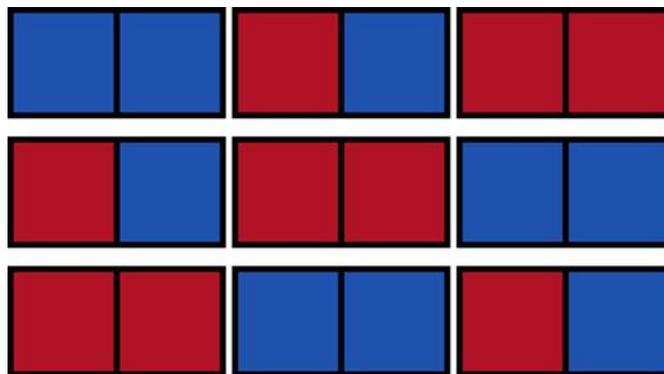


Fig. 4

- For the third domino set, $\{3,0,0,0\} \rightarrow \{1,0,1,1\}$

The rest of the sample testcases probably have many beautiful sequences, but the space won't be enough ☺.